

Challenge to model turbulence in tidally active seas

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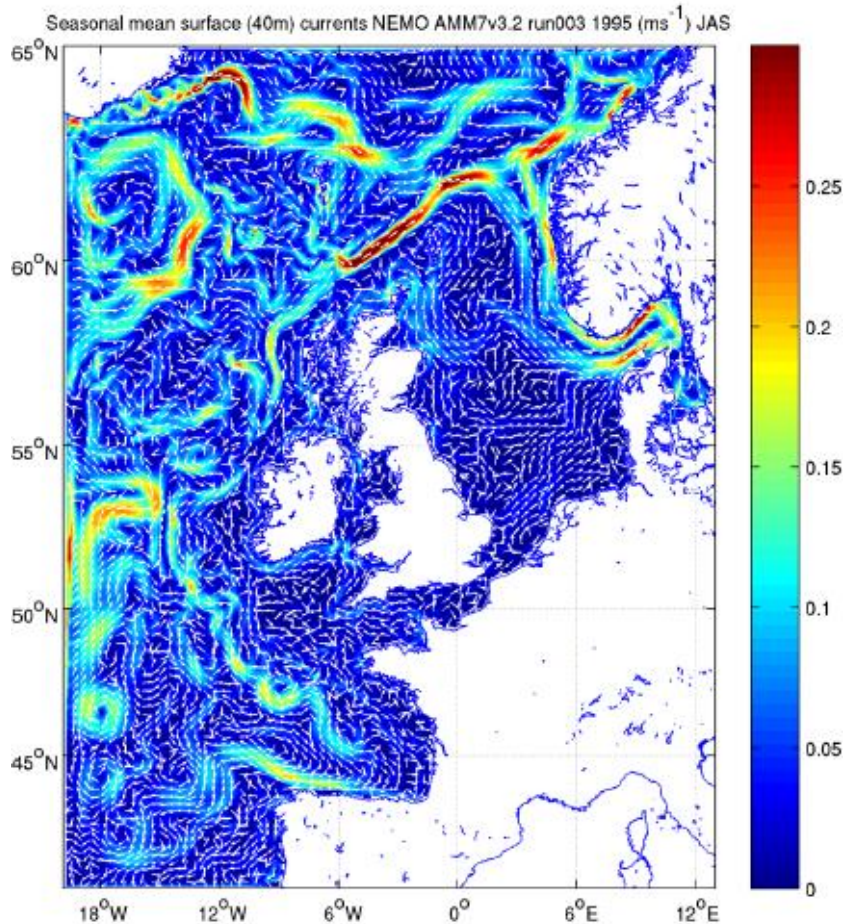


**National
Oceanography Centre**

NATURAL ENVIRONMENT RESEARCH COUNCIL

NERC SCIENCE OF THE
ENVIRONMENT

The Northwest European Continental Shelf



O'Dea et al 2012

Broad tidally dominated, downwelling shelf;
Borders subpolar and subtropical gyres

Strong mixing in winter
(shelf mixed over depth)
strong stratification in summer

MODEL: Nucleus for European Modelling
of the Ocean (NEMO)

- UK: NOC, Met Office
- France (MERCATOR), Italy

NEMO-shelf (O.Dea et al., 2012)

Domain:

Resolution: 7x7km, 51 vertical s-layers;

Forcing: IRA-interim surface flux

Boundary conditions: Global ORCA-25
runs, tides

Modelling period: 1996-2015, no
assimilations.

Model set up and comparison

- **Turbulence closure tested:** $k_{u,v,T,S} = ql S_{u,v,T,S}$
- **structural functions** $S_{u,v,T,S}$:

GA: Galperin et al, 1988

KC: Kantha Clayson, 1994

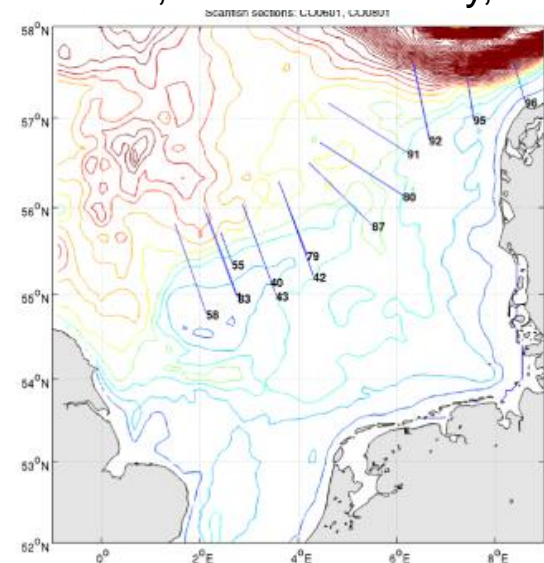
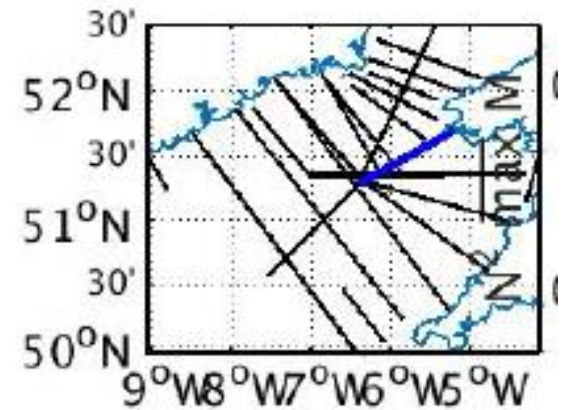
KC4 – KC with model constants from Kantha 2004, improved convection

CAA, Canuto et al, 2001

CAB, same but with different set of constants

!!! In all models surface parameterisations for breaking from Kantha, 2004 and Gerby, 2009. k-eps constants and equations fit observations at the

- $(\ell = \delta(z + 0.6H_s); \delta = 0.2 \neq \kappa)$
- **DATA:** High resolution scanfish sections
- Celtic Sea 1998, the North Sea, 2001
- **Turbulence observations in the Celtic Sea**
- 20 12-24 h long datasets of ε , N2
- years 1998 – 2013



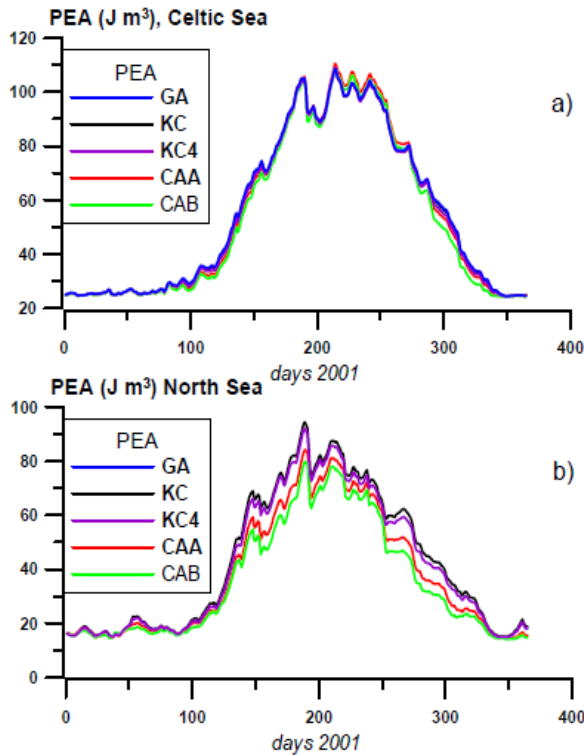
Model inter comparison

Potential Energy Anomaly:
Measure of stratification in water column

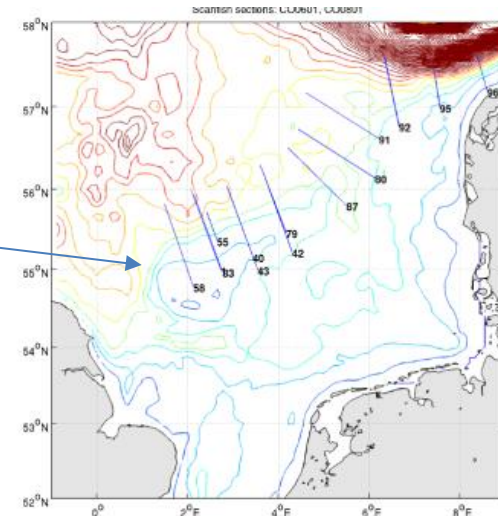
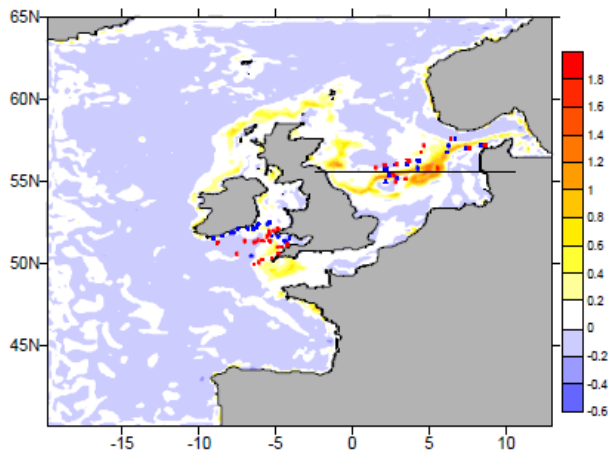
$$PEA = g \int_0^{\max(h, 200m)} (\rho - \rho_{mean}) z dz / \max(h, 200)$$

Shelf-mean differences are small,
locally large in the North Sea:
50-100%

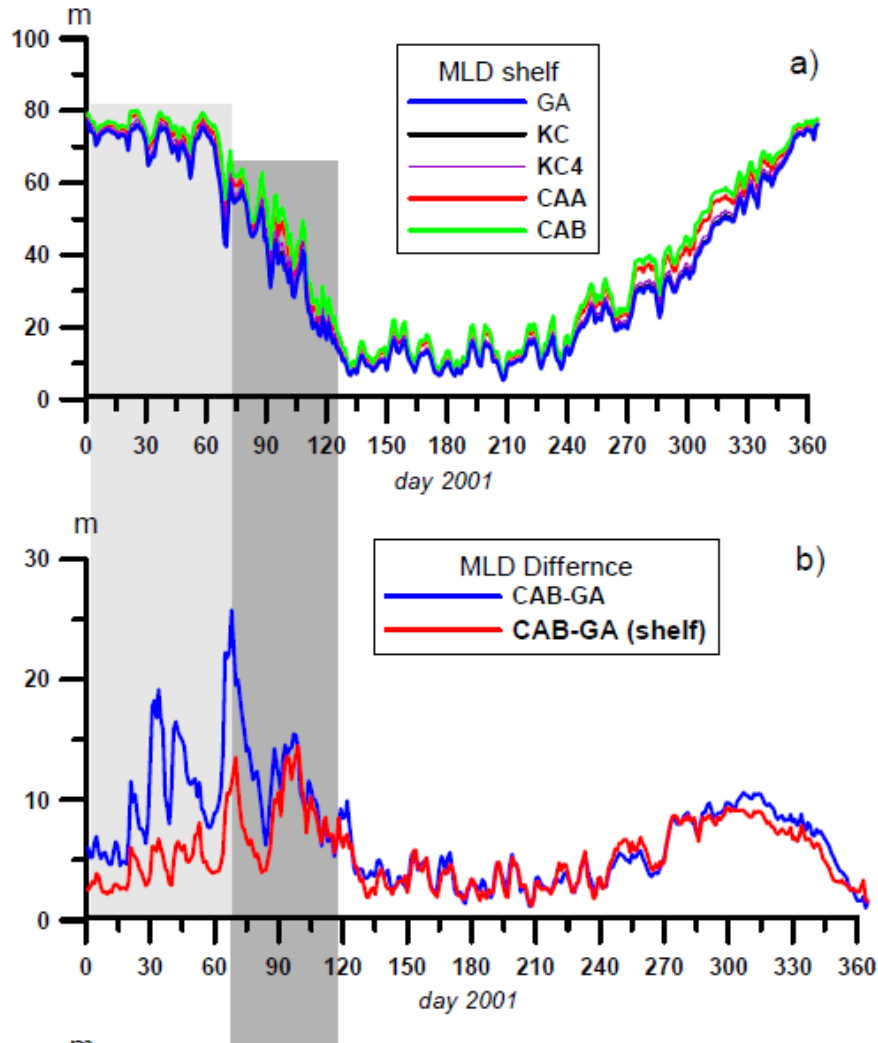
10



(PEA (KC) - PEA(CAB))/(PEA (KC) + PEA(CAB))



Model inter-comparison 1



Large differences in basin mean mixed layer depth:
 winter ~ 10-30%
 summer 25%

Turbulence closures can be sorted as

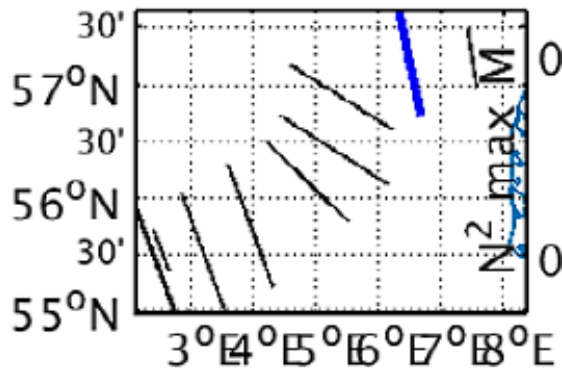
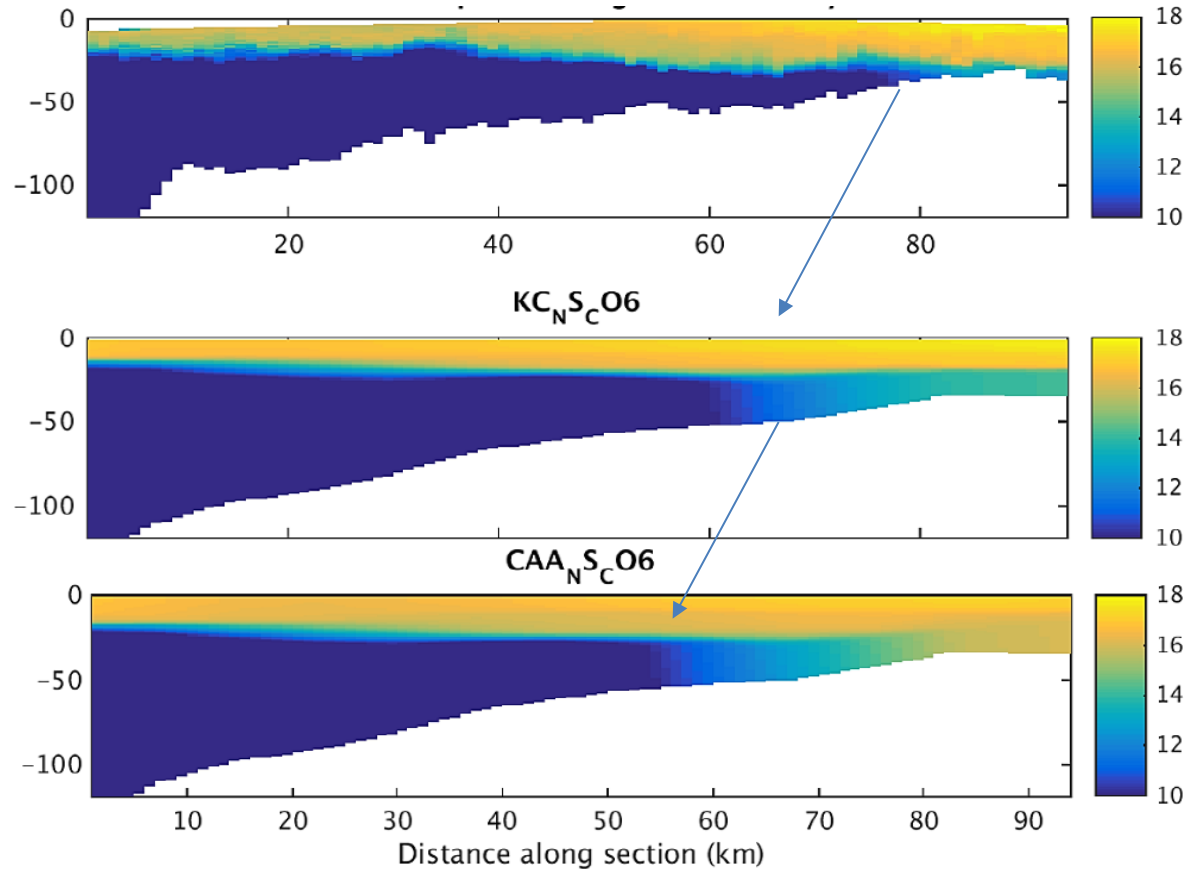
	GA	KC	KC4	CA	CAB
Ri_{cr} :	0.19	0.24	0.28	0.82	1.03

more diffusive →

Theoretically derived critical Ri / R_f correspond to Model gradation

Direct comparison with scanfish section: Across tidal mixing front

- shift of warm front with more diffusive model;
- absence of variability in pycnocline;
- Bottom boundary layer too thick?

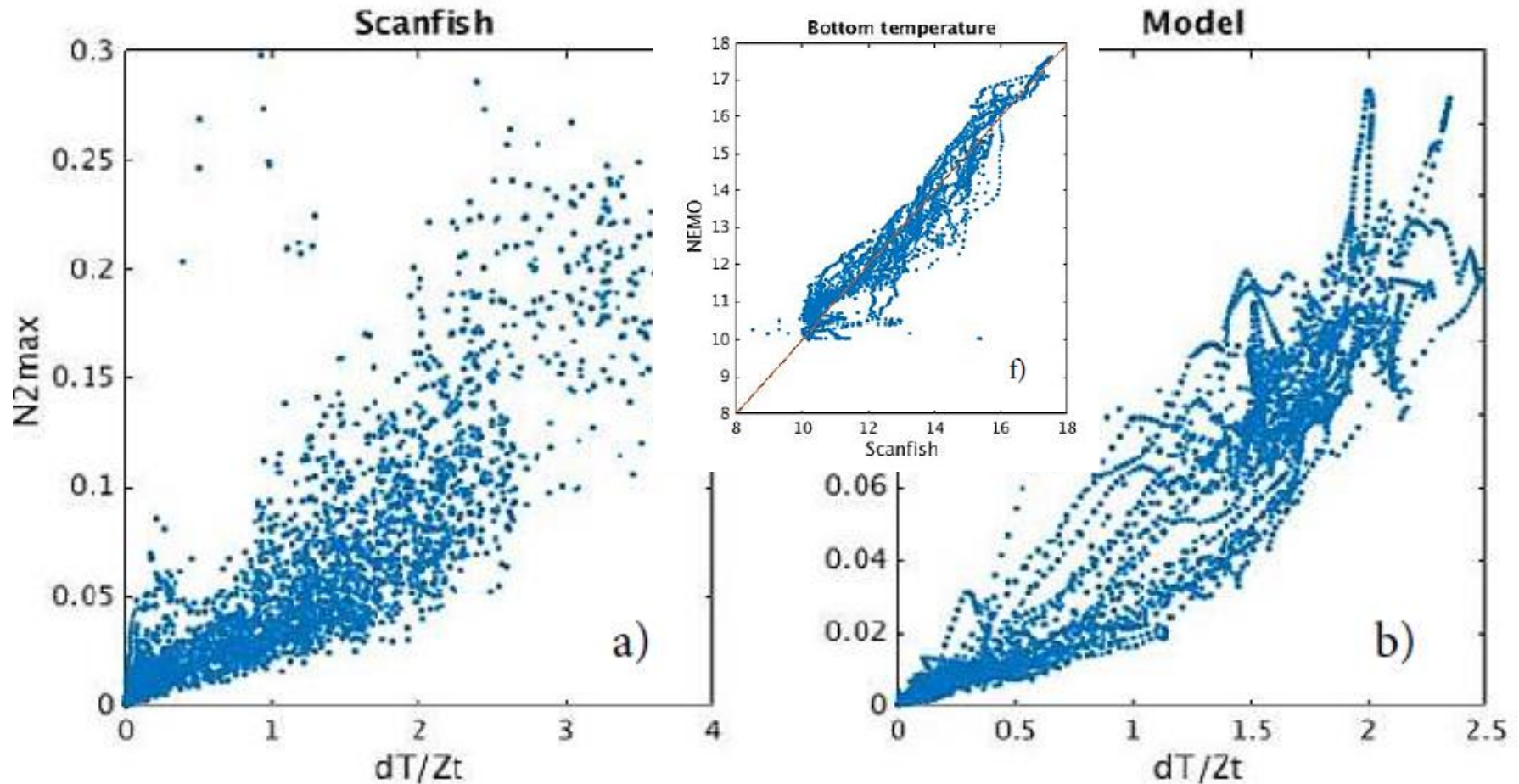


Local pycnocline properties versus integral:

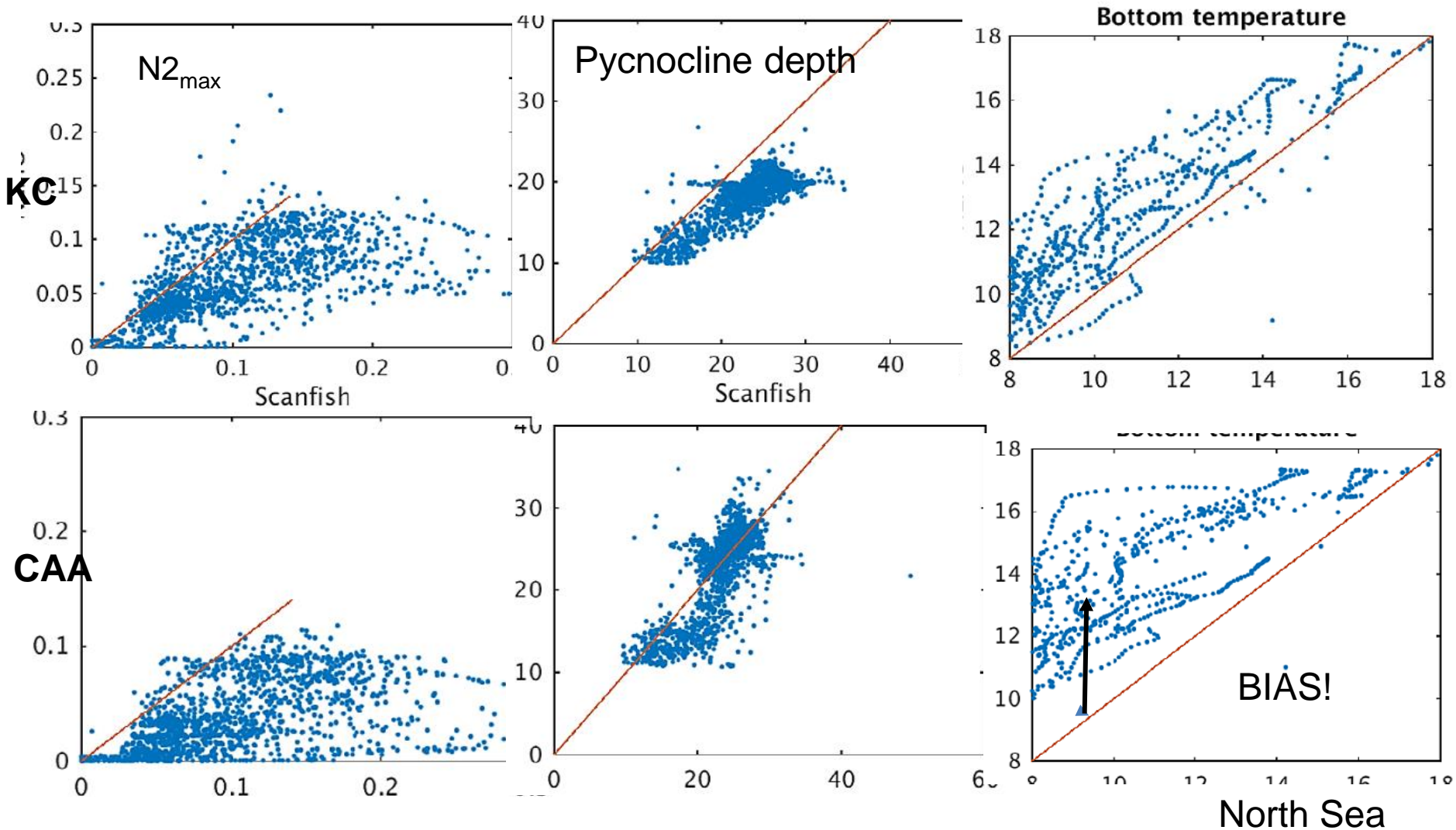
CS : $R(DT, Z_T * N2) = 0.5$

NS: $R(DT, Z_T * N2) = 0.7$

model : 0.85-0.9

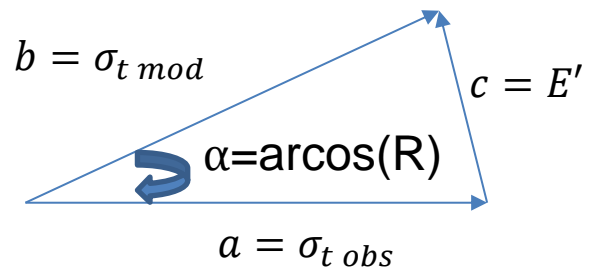


Direct comparison with scanfish sections: Overall statistics



Deficit in pycnocline depth(GA,KC) /or overmixing-warming (Canuto models)

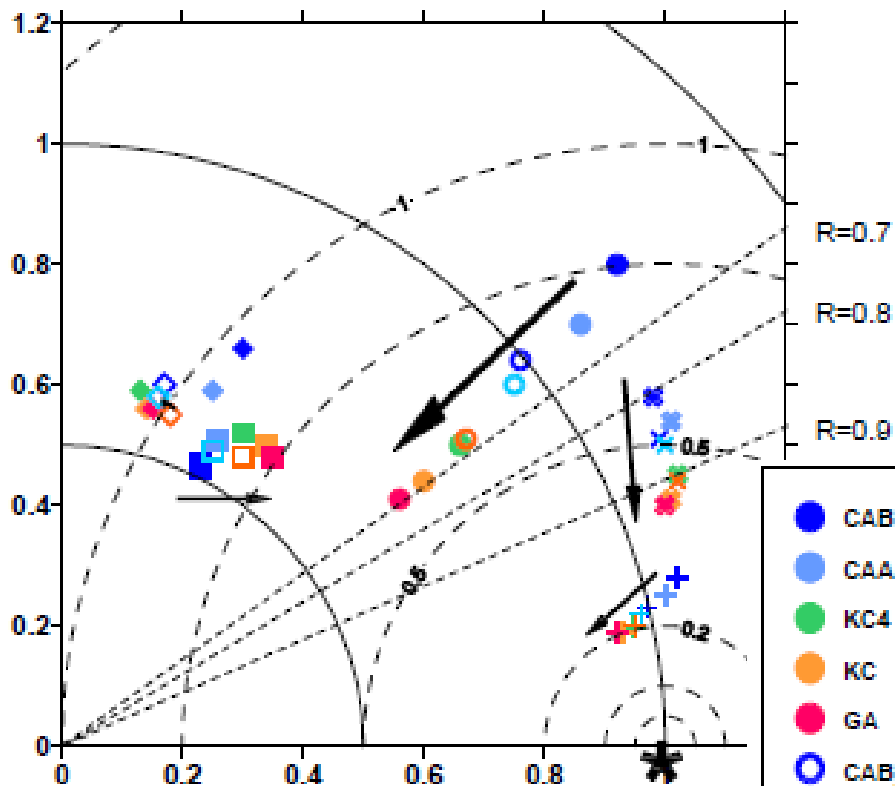
Taylor diagram: all variables on the same diagram.



$$c^2 = a^2 + b^2 - 2ab \cos \alpha$$

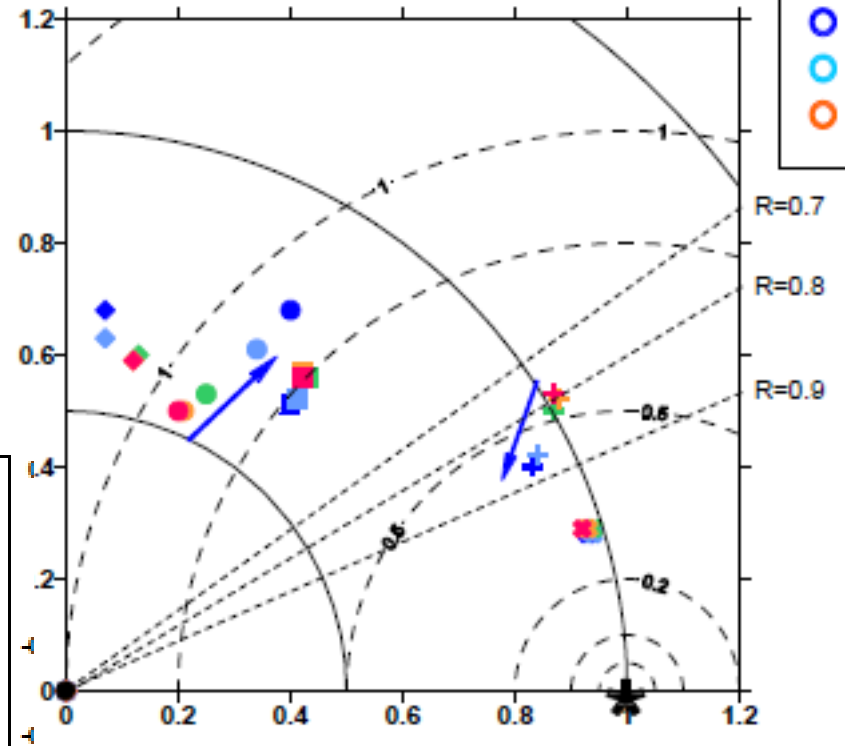
$$\frac{E'^2}{\sigma_{T0}^2} = 1 + \sigma_{Tm}^2/\sigma_{T0}^2 - 2\sigma_{Tm}/\sigma_{T0}R$$

NORTH SEA



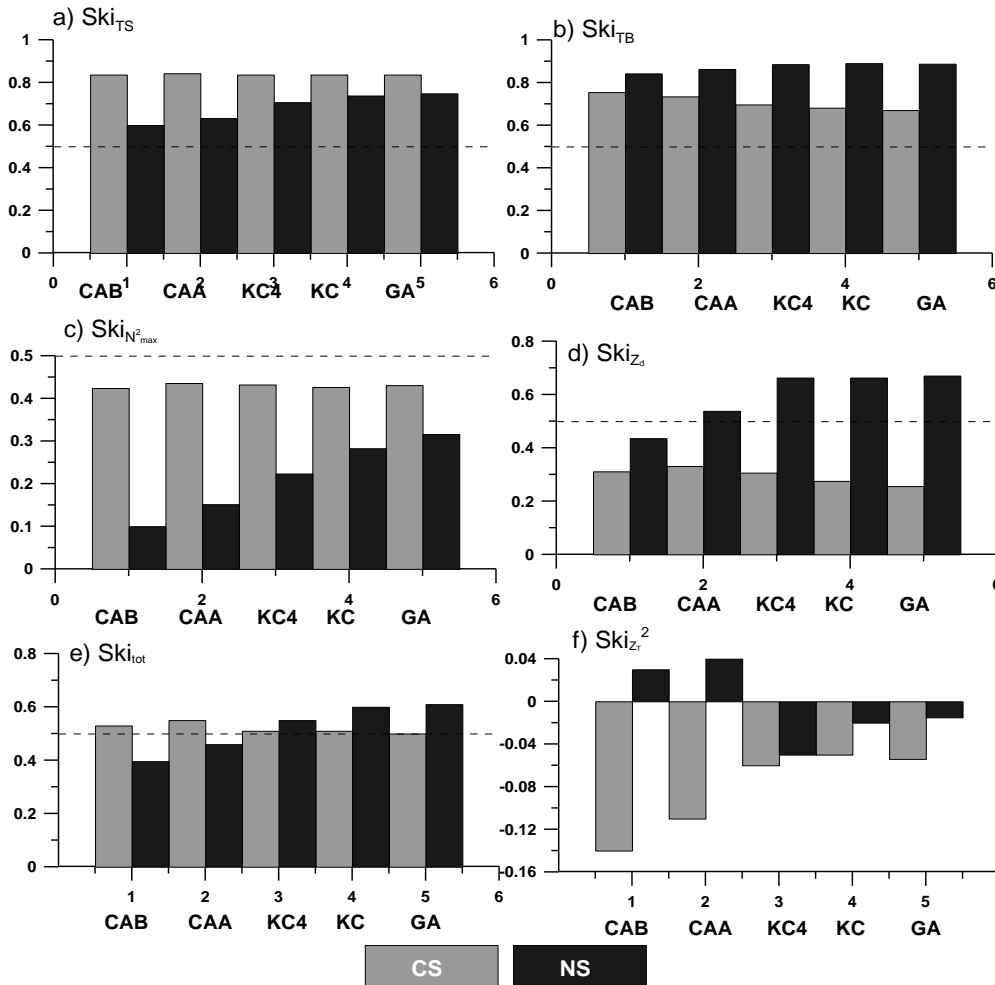
- CAB
- CAA
- KC4
- KC
- GA
- CAB_11
- CAA_11
- KC_11

CELTIC SEA



- + SST
- × SBT
- N2max
- Zd
- ◆ Zt

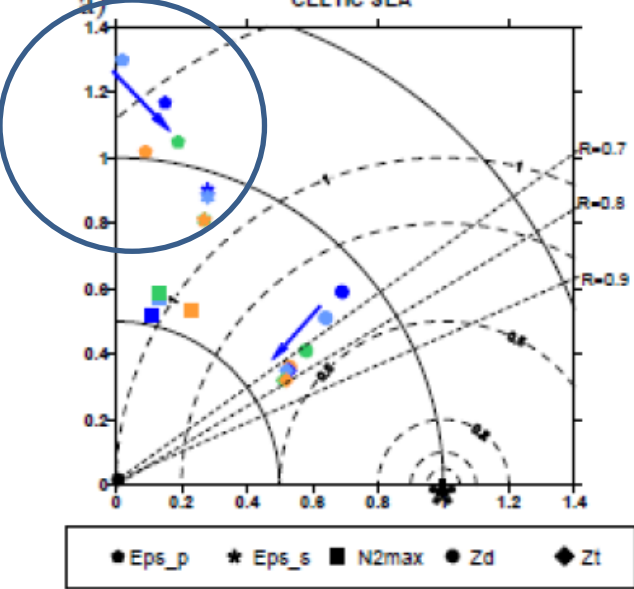
Taylor diagram evaluate only variability: How to evaluate 'model skill'?



$$Ski^i = \left\{ (1 - E') \left(1 - \frac{|M^i - O^i|}{|M^i| + |O^i|} \right) \right\}^{1/2}$$

$$Ski = \left\{ \prod_{i=1}^n Ski^i \right\}^{1/n}$$

Model skills for prediction of (a) SST, (b) SBT, (c) N^2_{max} , (d) Z_d , (e) total skill, (f) $Ski(Z_d)^2$. Grey- in the Celtic Sea, black- in the North Sea



Dissipation rate comparison: 20 datasets

- Dissipation rate comparison:
Subsurface layer :
an order underestimate;
Correlations ~0.3

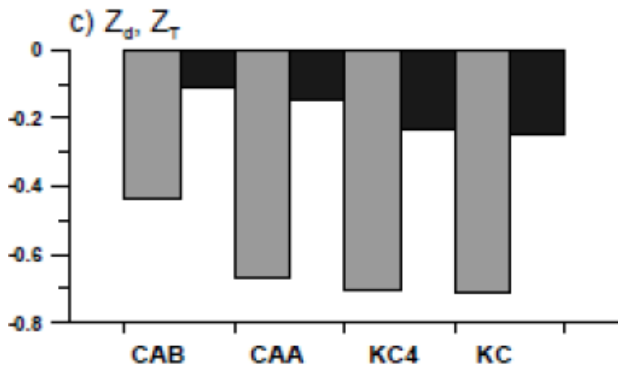
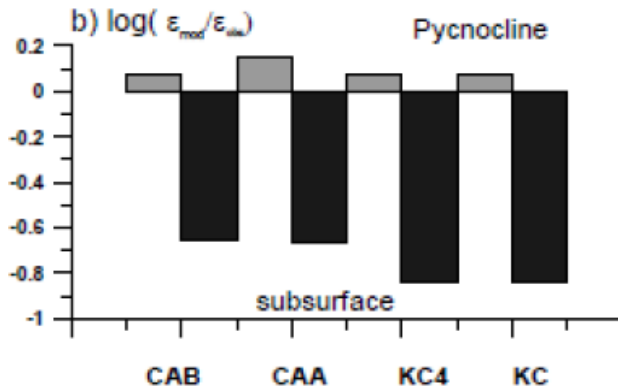
Pycnocline:

**overestimate on the shelf, by
order** Over-predicted mixing

$$K_v \sim \epsilon / N^2$$

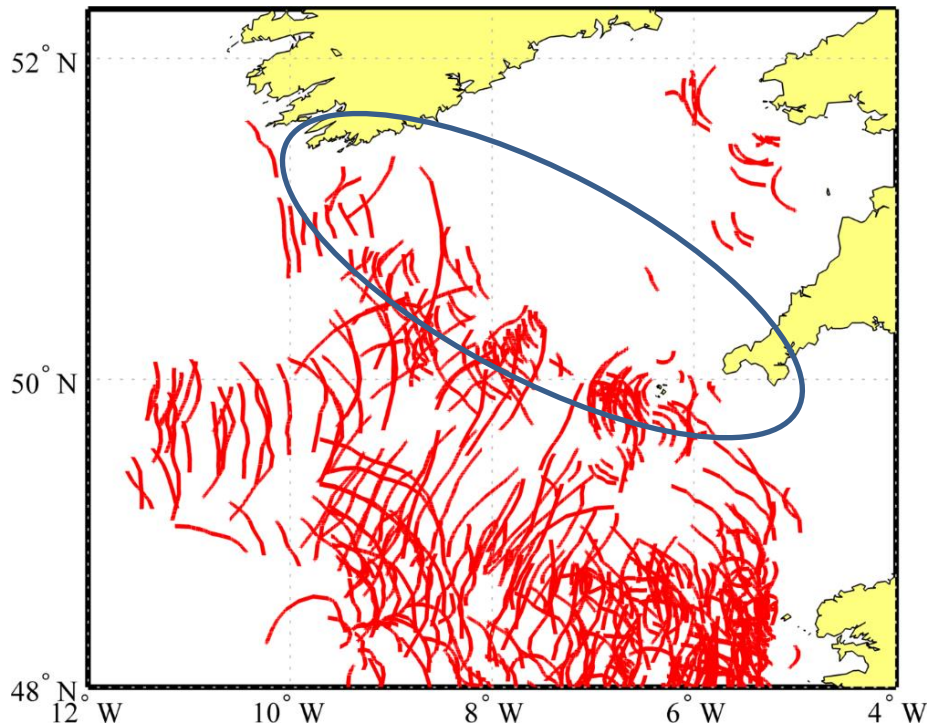
No correlations, relative error > 1

Underestimate on the Celtic Sea
shelf break (internal tides)



- (a) Taylor diagram dissipation data shown in circle
 (b) Relative biases from dissipation rate in log scale
 (c) For pycnocline thickness and depth in the Celtic Sea (grey is thickness), black pycnocline depth

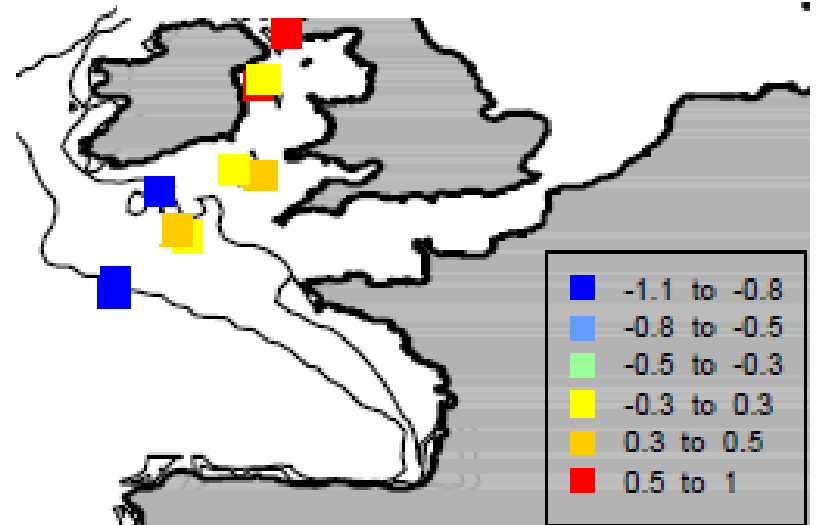
Images of steep Internal waves fronts (summer 2009)



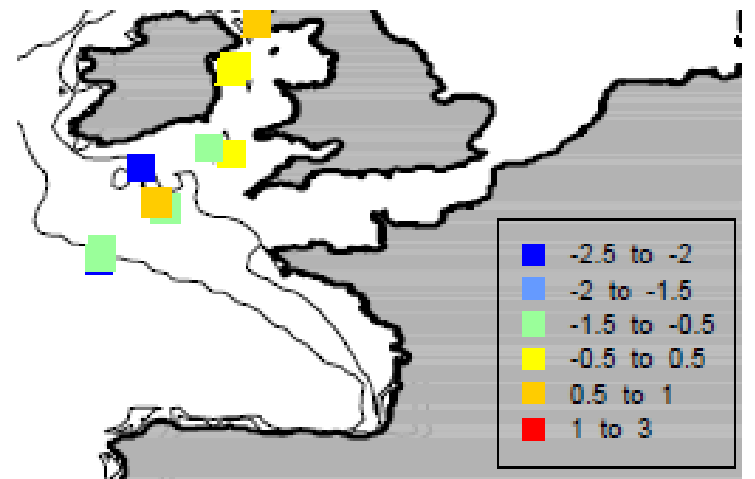
E Zubkova, I Kozlov

Steep solitary internal tides (summer 2008)
Breaking and dissipating, 344 packets

DISSIPATION RATE LOG10(MOD/OBS)
PYCNOCLINE

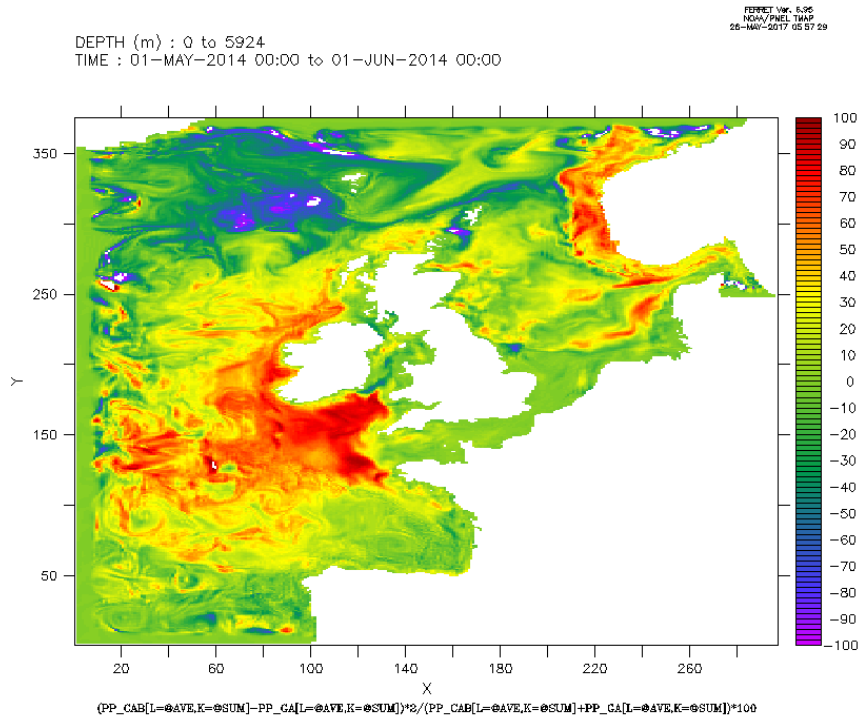


DISSIPATION RATE LOG10(MOD/OBS)
SUBSURFACE MAXIMUM

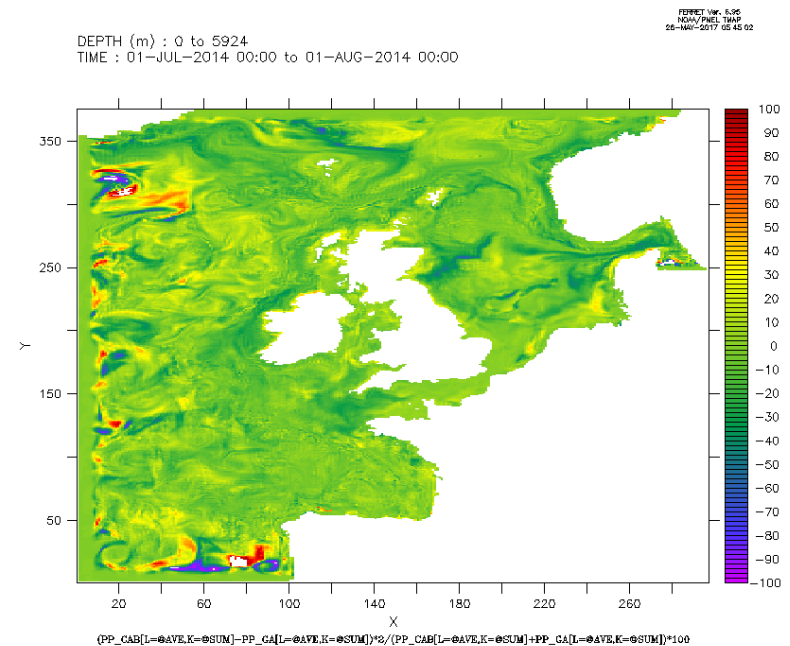


Effect on the Ecosystem

- ERSEM model, 3 closures 2014-2015!
- Just finished, ongoing comparison with data quit
- Differences reach 100%, sign changes in July



Chlorophyll: $(CAB-GA)/(CAB+GA)$
May 2014

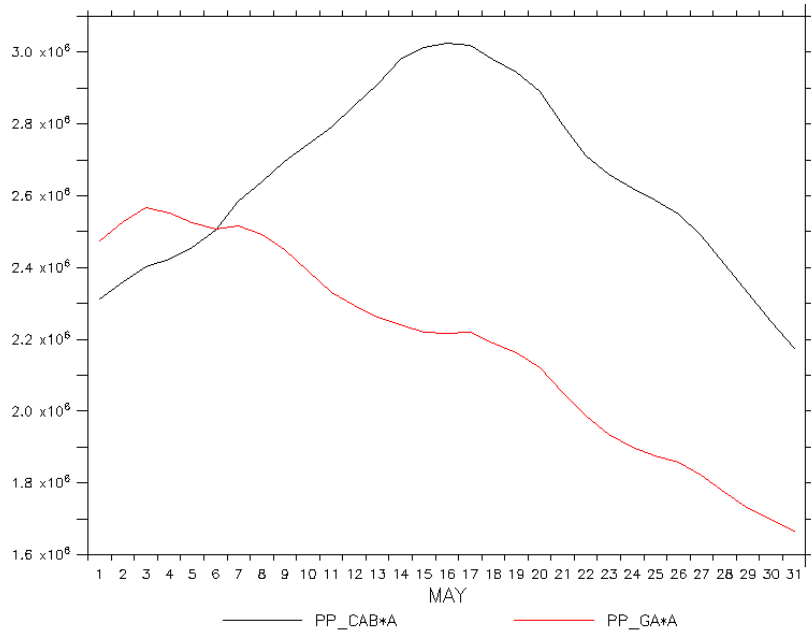


$(CAB-GA)/(CAB+GA)$
July 2014

Differences are stronger in May blooming (20%) CAB smaller in summer 10% with dominating GA (less diffusive model)

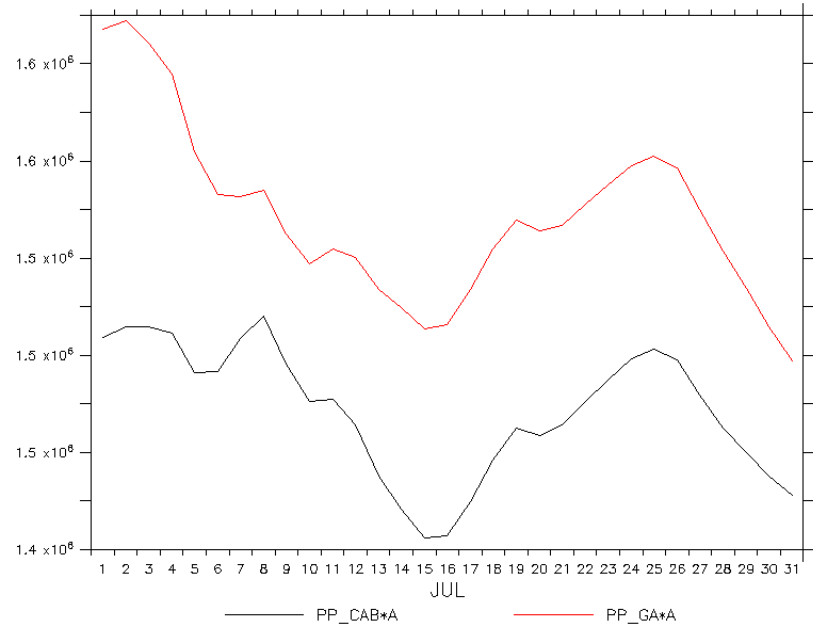
X : 0.5 to 297.5 (XYZ summed)
Y : 0.5 to 375.5 (XYZ summed)
DEPTH (m) : 0 to 5924 (XYZ summed)
YEAR : 2014

FERRET Vm. 6.96
NCA/PNEL THAP
26-MAY-2017 06:04:15



X : 0.5 to 297.5 (XYZ summed)
Y : 0.5 to 375.5 (XYZ summed)
DEPTH (m) : 0 to 5924 (XYZ summed)
YEAR : 2014

FERRET Vm. 6.96
NCA/PNEL THAP
26-MAY-2017 05:51:47



Nontraditional Coriolis: acts as buoyancy force

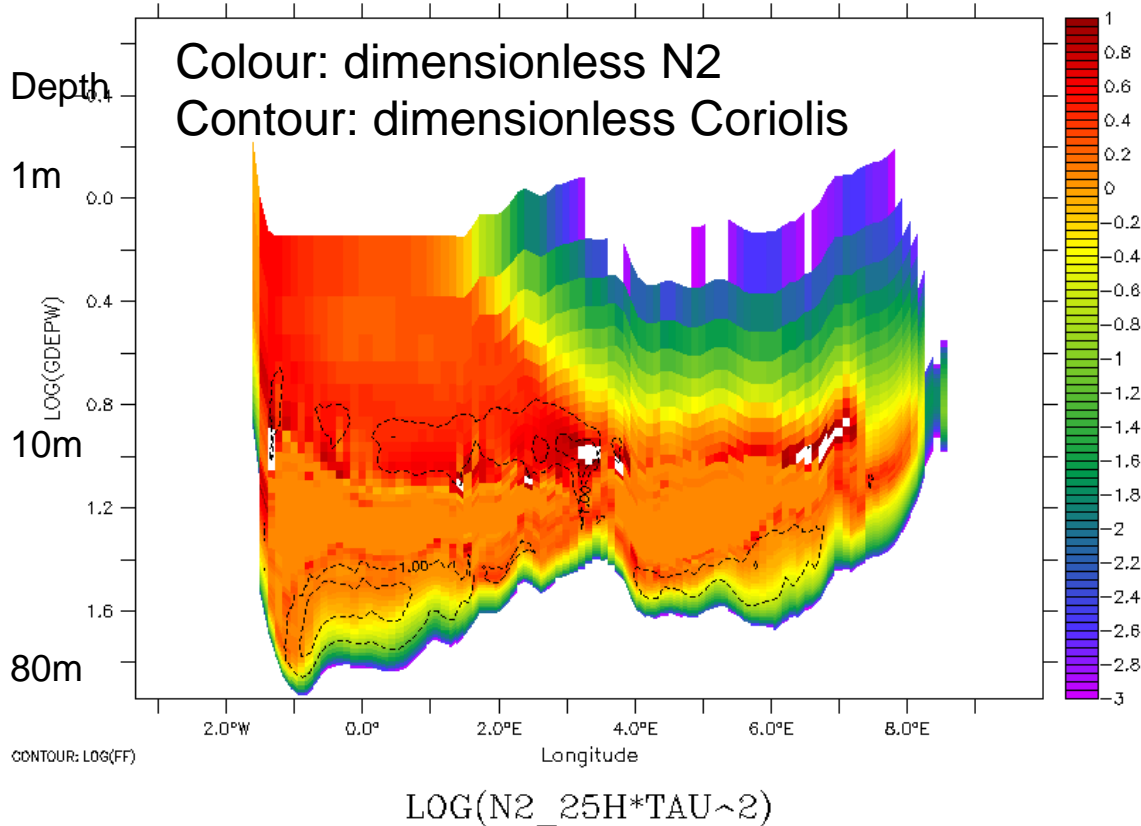
- $\varphi = \tau \partial_z U$, $\psi = \tau \partial_z V$, $f_0 = \tau f$, $h = \tau \check{f}$,
- $\tau = 2.7 q^{-1} l$ is a turbulent timescale, $q^2 = (u'^2 + v'^2 + w'^2)$
- Normalise $u^2 = u'^2 / q^2$
- *System of Equations in the “Equator”:*
 - $u^2 = \alpha - 2uw(\varphi + h)$
 - $v^2 = \alpha - 2vw(\psi)$
 - $w^2 = \alpha + 2uw h$
 - $uv = -uw\psi - vw\varphi - hvw$
 - $uw = -(w^2 - C_1)\varphi + h(u^2 - w^2)$
 - $vw = -(w^2 - C_1)\psi + huv$
- $uw = -\frac{(\alpha - C_1)\varphi}{1 + 4(\varphi + h)h}$; $S_{mu} = \frac{3A_1(\alpha - C_1)}{1 + 4(\varphi + h)h} \approx 0.39(1 - 4\varphi h)$
- If $\partial_z U > 0$: dumping , if $\partial_z U < 0$, works as unstable stratification

North Sea, July 2001

Y : 230
TIME : 01-JUL-2001 12:00

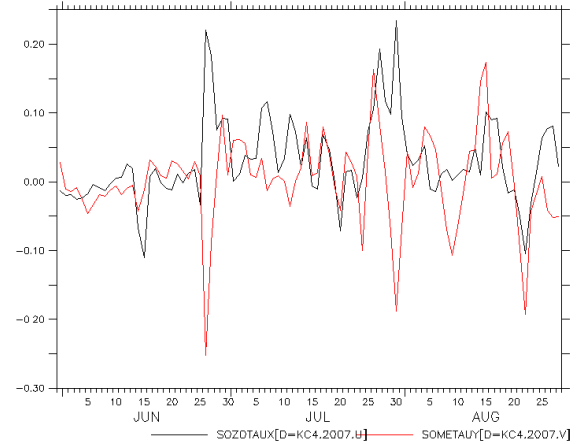
DATA SET: KC4_1d_20010701_20010731_grid_W
ocean W grid variables

FERRET Ver. 6.95
NOAA/PMEL TMAP
09-MAR-2017 13:27:34



X : 199.0 to 240.5 (XY ave)
Y : 19.5 to 240.5 (XY ave)
YEAR : 2007

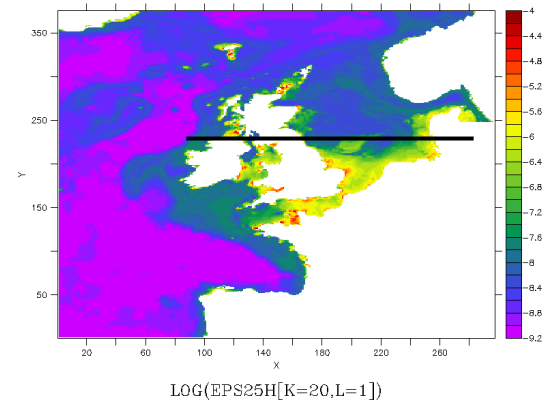
FERRET Ver. 6.95
NOAA/PMEL TMAP
09-MAR-2017 13:27:34



$$S_m \approx 0.39(1 - 4\phi h)$$

$$S_h?$$

DEPTH (m) : 419.4
TIME : 01-JUL-2001 12:00
DATA SET: KC4_1d_20010701_20010731_grid_W
ocean W grid variables



Dimensionless $N^2\tau^2$, contours $|\phi h| > 0.1$. What direction?

New closure, based on KC94 but with Coriolis effects-coming

- $u^2 = \alpha - 2uw(\varphi + h) + 2uvf_0$
- $v^2 = \alpha - 2vw(\psi) - 2uvf_0$
- $w^2 = \alpha + 2uw(h) + 2w\theta$
- $uv = -uw\psi - vw(\varphi) - f_0(u^2 - v^2) - f_2vw$
- $uw = -(w^2 - C_1)\varphi + f_0vw + h(u^2 - w^2) + u\theta$
- $vw = -(w^2 - C_1)\psi - f_0uw + huv + v\theta$
- $u\theta = -uw\chi - \frac{A_2}{A_1}(1 - C_2)w\theta\varphi + \frac{A_2}{A_1}f_0v\theta - \frac{A_2}{A_1}h w\theta$
- $v\theta = -vw\chi - \frac{A_2}{A_1}(1 - C_2)w\theta\psi - \frac{A_2}{A_1}f_0u\theta$
- $w\theta = -w^2\chi - \frac{(1-C_3)}{3}B_2w\theta\chi + \frac{A_2}{A_1}h u\theta$

Require solution of 9 algebraic equations in 4D parameter space.

Now system is reduced to 3 equations in the linear approximation for h.

Missed process 1. Shrira Forget, 2015

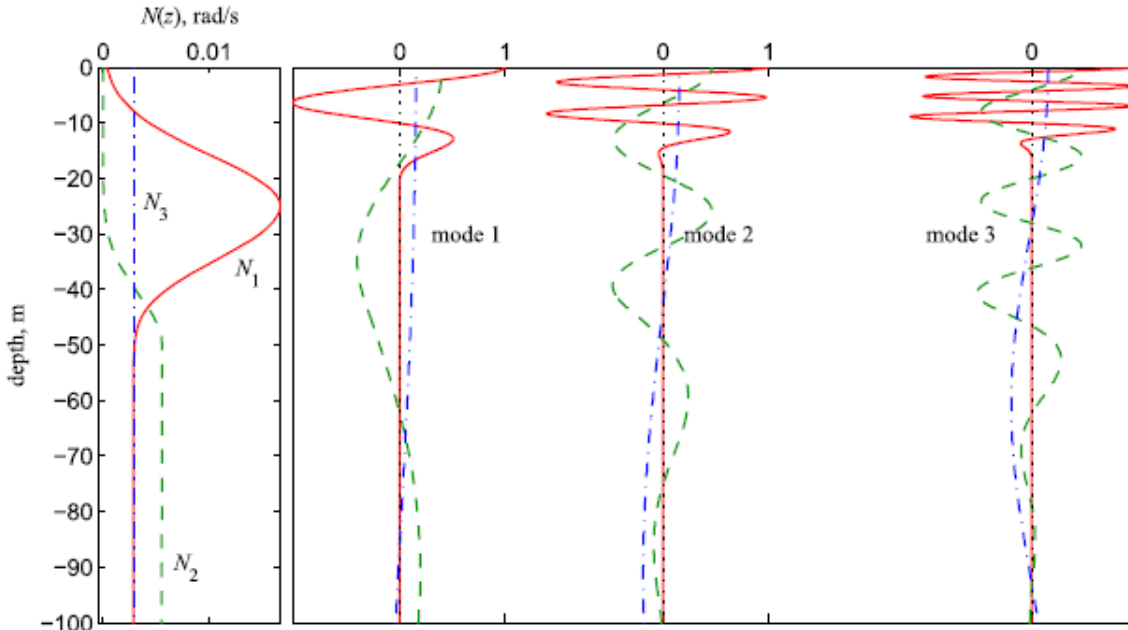


FIG. 1. (left) Three samples of stratification profiles $N_1(z)$, $N_2(z)$, and $N_3(z)$. The full water column depth in the chosen example is 400 m, but only the uppermost 100 m is shown; profiles are shown in full in Fig. 2. (right) An example of vertical distribution of horizontal velocities for the first three subinertial modes for the chosen sample stratification profiles. The horizontal velocities are found from the linearized Euler equations with $f = 0.99 \times 10^{-4} \text{ rad s}^{-1}$ and $\bar{f} = 1.06 \times 10^{-4} \text{ rad s}^{-1}$. The plots are for a sample frequency from the subinertial range ($\omega = 0.898 \times 10^{-4} \text{ rad s}^{-1}$), and the corresponding meridional wavenumbers l (rad m^{-1}) are 9.46×10^{-5} , 2.2×10^{-4} , and 3.44×10^{-4} for $N_1(z)$; 1.72×10^{-5} , 4.58×10^{-5} , and 7.40×10^{-5} for $N_2(z)$; and 3.55×10^{-6} , 7.1×10^{-6} , and 1.106×10^{-5} for $N_3(z)$.

Most frequently observed when strong wind stops or changes in direction

Non-traditional NIW:

Found in analytical solutions

Observed in the stratified ocean

Cannot penetrate through pycnocline!

Generate strong shear

Cannot be resolved in hydrostatic models

Additional shear can be parameterised using wind forcing

$$u_t - fv + \tilde{f}w = -p_x, \quad (1a)$$

$$v_t + fu = -p_y, \quad (1b)$$

$$w_t - \tilde{f}u = -p_z + b, \quad (1c)$$

$$u_x + v_y + w_z = 0, \quad \text{and} \quad (1d)$$

$$b_t + N^2w = 0. \quad (1e)$$

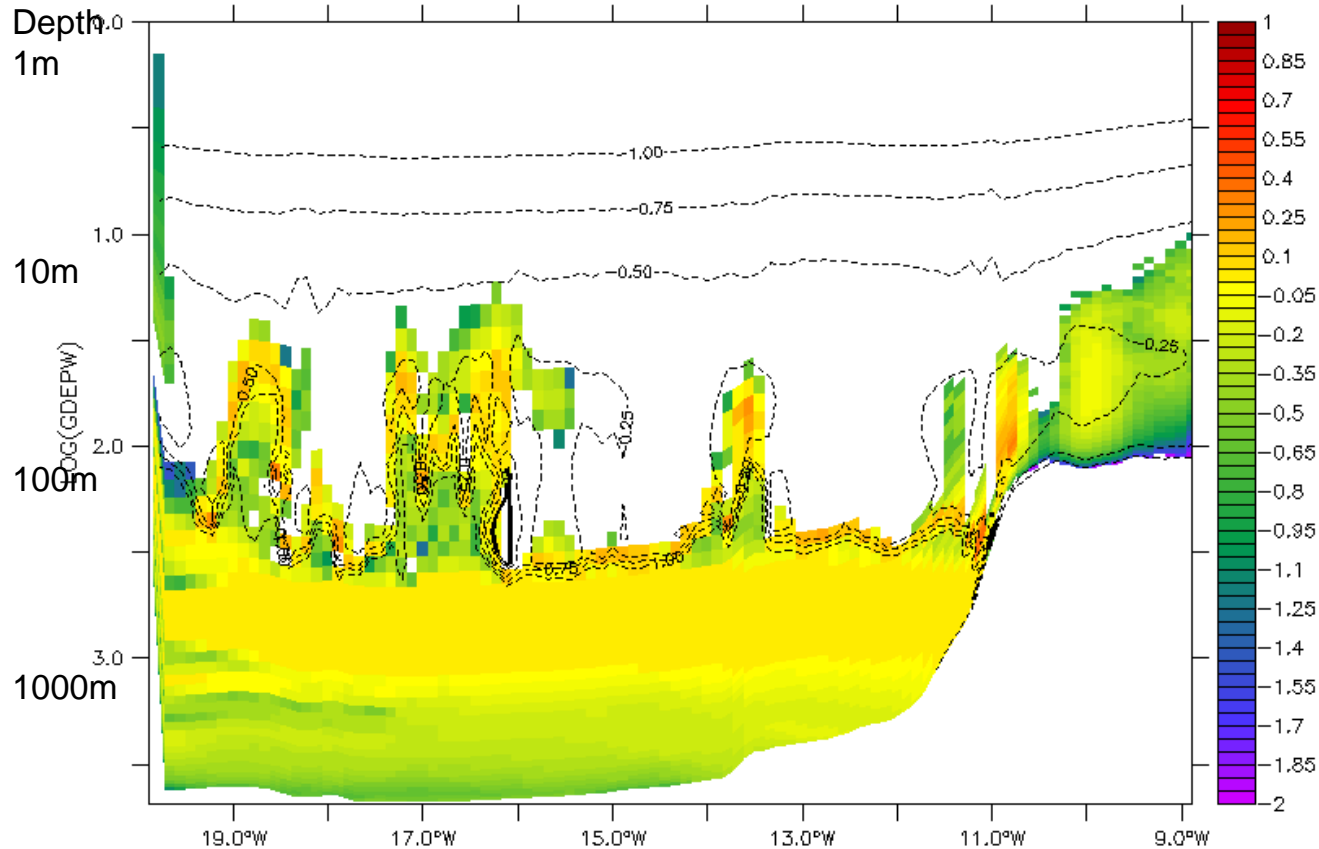
Conclusions

- The choice of structural functions does matter!
- Strong differences in blooming time
- More diffusive model spent nutrients much faster
- Differences in structural functions are essential for ecosystem
- Comparing with turbulence measurement are very poor
- No winners between models, more diffusive work better in active seas
- Less diffusive models work better in the shy seas
- Non-traditional Coriolis force acts as stratification- should be included in models

The Celtic Sea, March

FERRET Ver. 8.65
NOAA/PMEL TRMP
08-MAR-2017 18:34:42

Y : 150
TIME : 01-MAR-2010 12:00 DATA SET: KC4_1d_20100301_20100331_grid_W
ocean W grid variables



CONTOUR: LOG(S2_25H~0.5*1.E-4*TAU~2)/2

LOG(N2_25H*TAU~2)/2

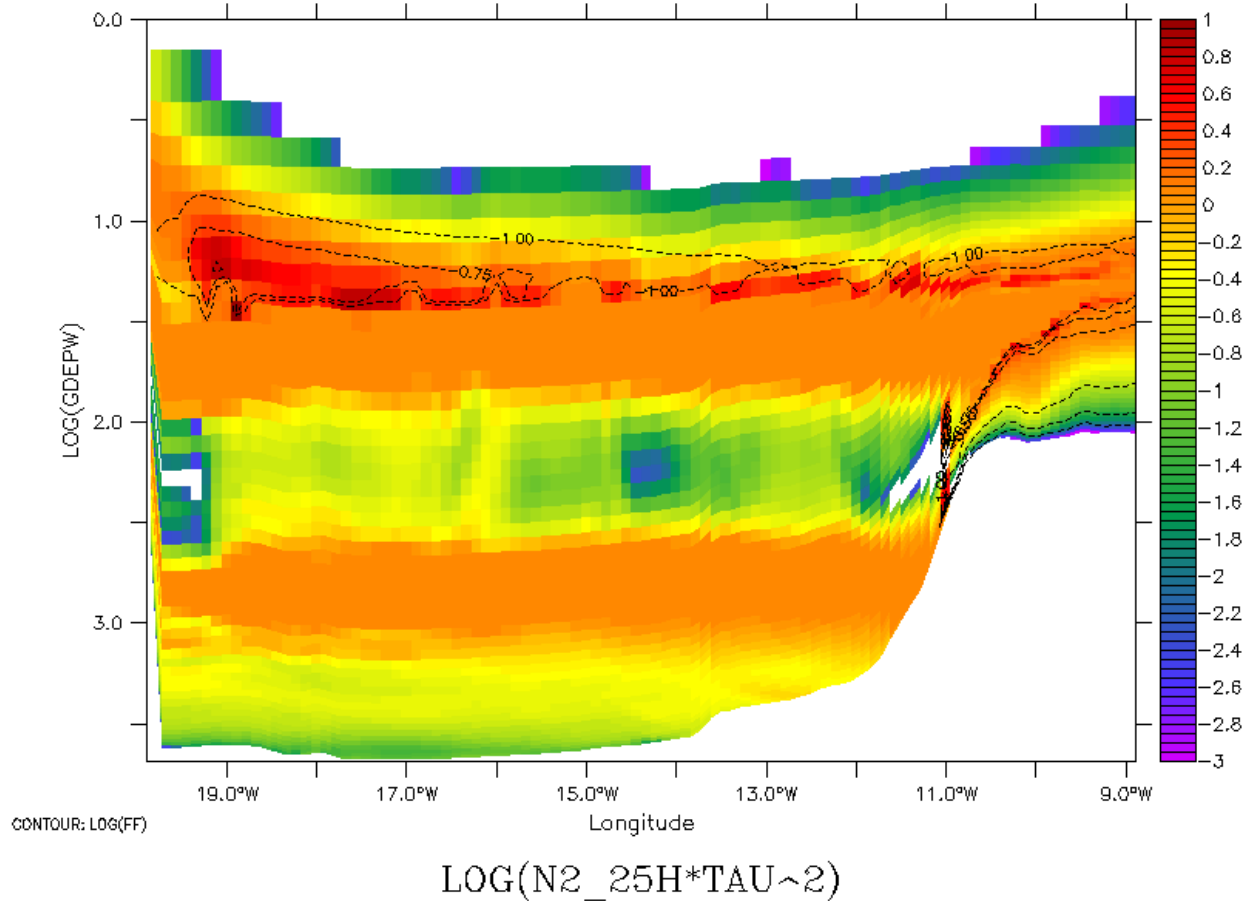
Non-traditional Coriolis effects could be to be very strong: $h\phi \sim 0.6$

The Celtic Sea, May

FERRET Ver. 8.05
NOAA/PMEL TMAP
08-MAR-2017 13:21:24

Y : 150
TIME : 01-MAY-2010 12:00

DATA SET: KC4_1d_20100501_20100531_grid_W
ocean W grid variables



The Celtic Sea

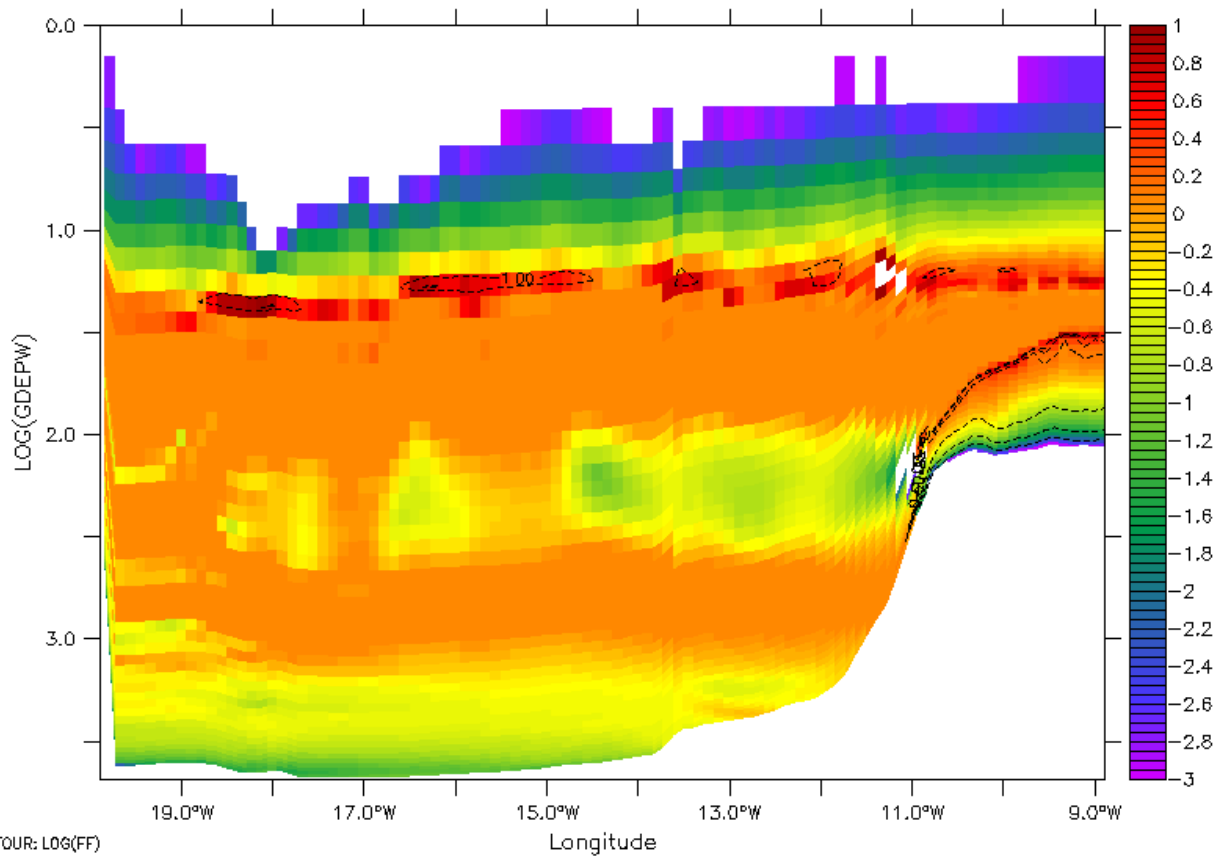
FERRET Ver. 8.05
NCAR/PMEL TRAP
09-MAR-2017 13:08:29

Y : 150

TIME : 01-JUL-2010 12:00

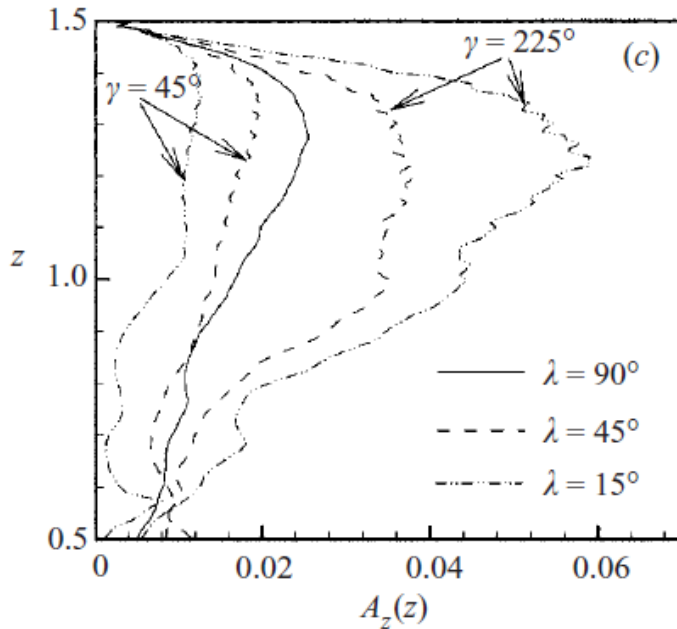
DATA SET: KC4_1d_20100701_20100731_grid_W

ocean W grid variables



$\text{LOG}(N^2_{25H} \cdot \tau^{-2})$

“nonstandard” Coriolis effects II



validated versus LES (Zikanov et al, *J.Fluid Mech.* 2003)

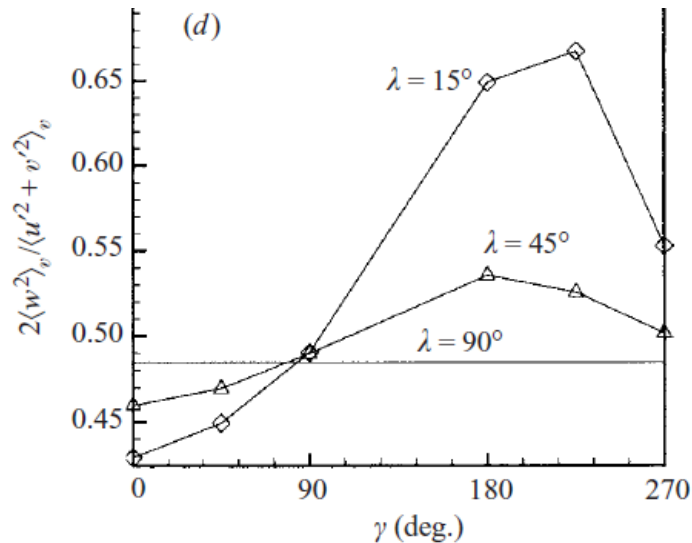
$$\frac{1}{2} \frac{\partial}{\partial t} \langle u'^2 \rangle = -\frac{\partial U}{\partial z} \langle u'w \rangle - 2\Omega_{\tau y} \langle u'w \rangle + \text{OT},$$

$$\frac{1}{2} \frac{\partial}{\partial t} \langle v'^2 \rangle = -\frac{\partial V}{\partial z} \langle v'w \rangle + 2\Omega_{\tau x} \langle v'w \rangle + \text{OT},$$

$$\frac{1}{2} \frac{\partial}{\partial t} \langle w'^2 \rangle = 2\Omega_{\tau y} \langle u'w \rangle - 2\Omega_{\tau x} \langle v'w \rangle + \text{OT},$$

$$-\frac{\partial}{\partial t} \langle u'w \rangle = -2\Omega_{\tau y} [\langle u'^2 \rangle - \langle w'^2 \rangle] + \text{OT},$$

$$\frac{\partial}{\partial t} \langle v'w \rangle = -2\Omega_{\tau x} [\langle v'^2 \rangle - \langle w'^2 \rangle] + \text{OT}.$$



- Redistribute energy over components differently
- Result in strong anisotropy of TKE
- direction of wind-latitude γ is important
- (here λ is latitude)
- 6-fold changes in diffusivity $A(z)$.

$$A_z(z) = \frac{[\langle -\tau_{13} + u'w \rangle_t^2 + \langle -\tau_{23} + v'w \rangle_t^2]^{1/2}}{[(d\langle u \rangle_t/dz)^2 + (d\langle v \rangle_t/dz)^2]^{1/2}}.$$